

faces directly away from chassis center-point. A dimensioned schematic of such a chassis is provided in Figure 1.

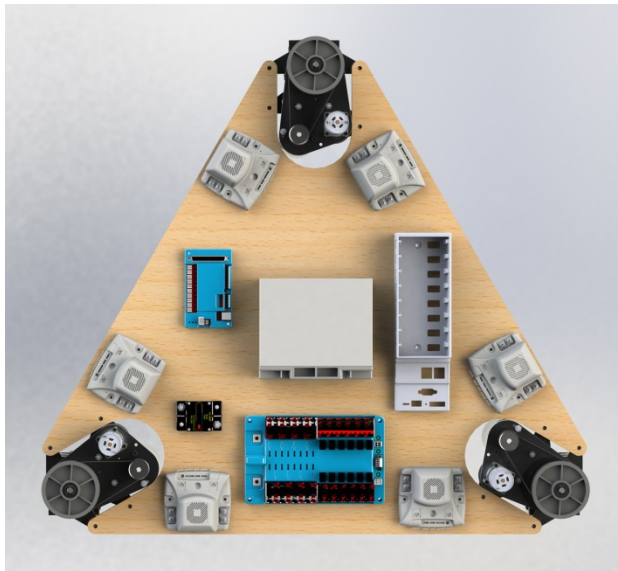
Conventions

In this document, lengths will be expressed in inches (in or ") and angles in degrees (°). Longitudinal precision will be 0.001" unless stated otherwise.

Right-hand rule applies for determining positive angle direction.

Swerve angles will be based on single-direction drive with each module's drive direction being the swerve angle direction (therefore driving at 0° when the swerve angle is 0°).

Prototype



A Tribot prototype chassis was designed and built using 3/4" thick laser-cut plywood. An 8-slot cRIO was employed due to ready availability. Jaguar motor controllers were elected for the same reason. The design called for 2013 swerve modules, but 2012 modules were actually installed, again due to ready availability. The 2012, 2013 & 2014 swerve modules share identical mounting bolt hole patterns (the 2012 having an additional, unused mounting hole) and identical relations between these mounting holes and the pivot, CIM and steering axes, so critical geometry is unaffected. The 2012, 2013 & 2014 swerve

modules also utilize the same angle sensors, and these are mounted in the same manner.

The Tribot prototype maintains the same swerve module spacing and orientations as provided in the Figure 1 schematic on Page 1.

Human Interface

The Driver uses a wired Xbox controller having dual, thumb-driven joysticks.

The primary joystick controls the robot's movement in *Crab Mode*.



In **Crab Mode**, both x and y information is used with the joystick's angle providing directional settings and the joystick's displacement from neutral providing speed settings.

The secondary joystick works with the primary to provide the turning capabilities of **Snake** and **Ocelot Modes**. Only the x information is used from the secondary joystick and this indirectly sets turning radius.

Chassis-centric versus Field-centric control

Chassis-centric and field-centric refer to two different directional references for the driver and the control logic. Team 1640 has hitherto always used chassis-centric control in which a specific axis of the chassis is determined to be "straight ahead". Joystick controls then operate on this reference. This is easier to execute from an instrument and software basis, as it does not require the robot to "know" which way it is facing relative to the field axes. On the other hand, it required the driver to know which way the robot is facing relative to field axis and to put her/his mind into this orientation while driving. This increases the driver's mental burden.

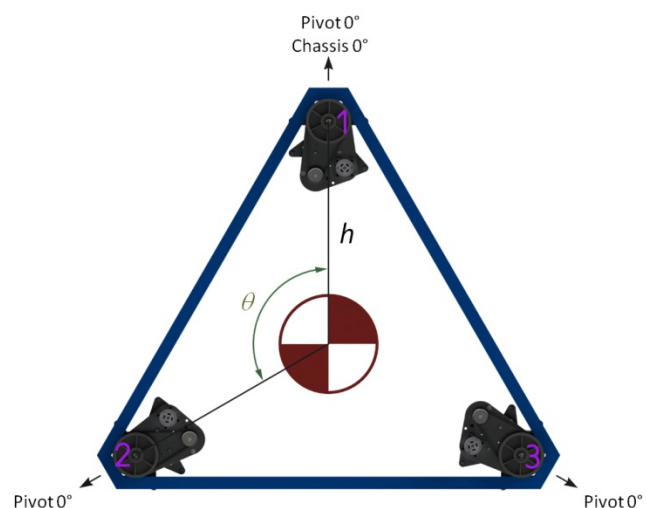
Field-centric control would allow the driver to move the robot around the field using the primary joystick while controlling the chassis orientation relative to the field with the secondary. The driver's reference space becomes the stationary field, reducing (we think) driver's mental burden. From a robot standpoint, life gets harder, as the robot now needs to "know" its orientation relative to the field. Gyroscopes are the way to know this and only one axis is needed. Issue is that the gyroscope must remain stable for the match duration (with all its hard knocks) to be effective.

Other than the change in reference, **Crab Mode** remains the same in chassis and field-centric control. The same is not true for **Snake** and **Ocelot**, as these undergo a reversal. In chassis-centric control, **Snake Mode** is static whereas **Ocelot** requires dynamic driver input. These relationships flip in field-centric control.

Chassis-centric control will be derived first; Field centric follows because it applies an additional level of calculation and control to Chassis-centric logic.

Chassis Geometry

Remaining consistent with both Figure 1 on Page 1, the actual prototype, and (as far as possible) previous white papers by this author, three swerve modules are arranged around a chassis center-point with a uniform distance h between the chassis

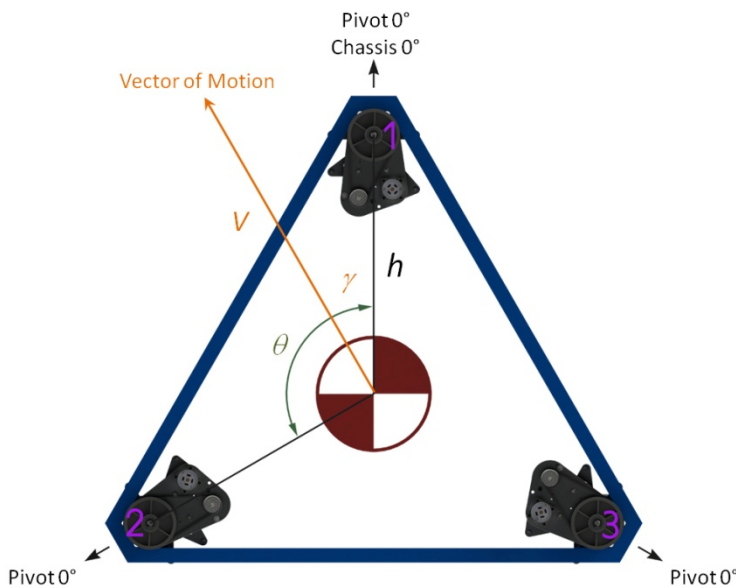


center-point and the pivot axes and an angle $\theta = 120^\circ$ ($2\pi/3R$) between each pivot axis around the chassis center-point. Swerve modules are mounted so that each module's 0° calibration axis faces directly away from the chassis center-point. Swerve modules are identified by numbers 1, 2 & 3 following right-hand rule.

The line from the chassis center-point to the pivot axis of swerve module 1 defines the 0° chassis axis.

Note that based on Figure 1, $h = 17.762$ in.

Chassis-Centric Crab Mode



In *Crab Mode*, the primary joystick applies a *Vector of Motion* to the chassis described in the previous section. This *Vector of Motion* provides both angular direction (γ) and power/speed (V) information.

γ may be $0-360^\circ$.

For Crab Mode, all swerves would be aligned with γ . For individual swerve angles (α_{Ci}):

$$\alpha_{C1} = \gamma \quad \text{eq. 1}$$

$$\alpha_{C2} = \gamma - 120^\circ \quad \text{eq. 2}$$

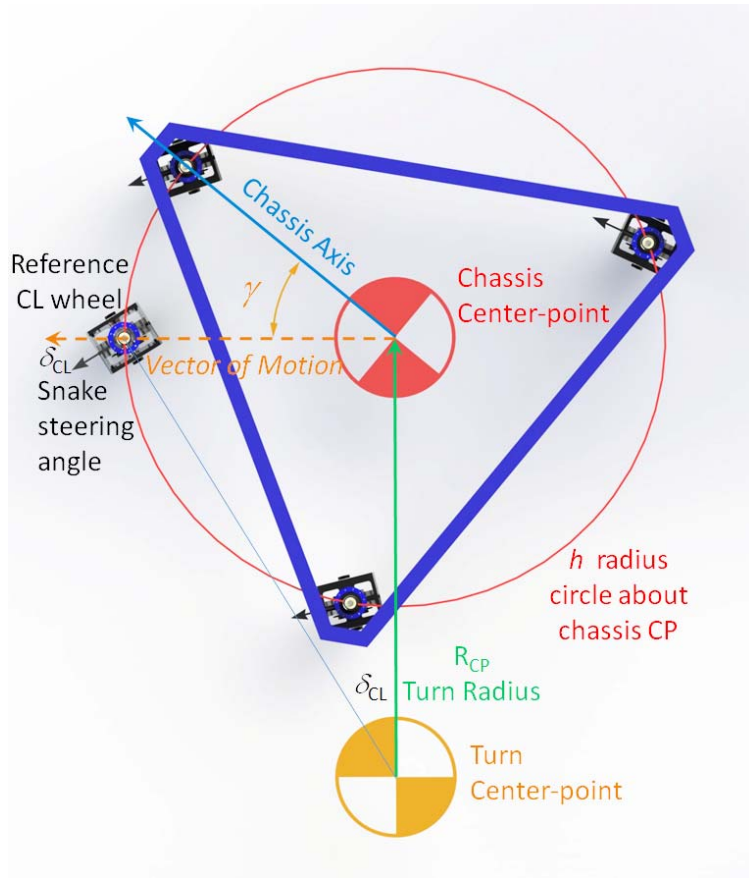
$$\alpha_{C3} = \gamma - 240^\circ \quad \text{eq. 3}$$

All calculated swerve angles must be checked and if $<0^\circ$, add 360° to make $>0^\circ$. However, the right time to make this correction (and the opposite: if $>360^\circ$, subtract 360° to make $<360^\circ$) is after assessing all drive calculations, including *Snake Mode*.

Drive power (V) is proportional to the primary joystick's displacement from neutral. In *Crab Mode*, all drives receive equal power.

Chassis-Centric Snake Mode

Snake Mode drives the chassis in an arc with chassis orientation following the path of the arc. The basic chassis orientation and speed are based upon the *Crab Mode* primary joystick inputs, while the arc radius is indirectly set via the secondary joystick x input.



In the 2009 swerve white papers, I introduced the concept of a "reference CL wheel", a useful tool for working through the mathematics around Snake Mode. The "reference CL wheel" concept will be employed again here.

The "reference CL wheel" is not a real wheel, but a hypothetical pivot wheel located at a distance h from the chassis center-point and oriented along the *vector of motion*. The diagram at left shows a "reference CL wheel" and the real pivot wheels on a chassis.

The secondary joystick steers by steering the reference CL wheel directly, creating an angle, δ_{CL} , between the *vector of motion* and the reference CL wheel's drive

direction. It can be easily shown that the triangle formed by the reference CL wheel, the chassis CP and the Turn CP is a right triangle and has the angle δ_{CL} at the Turn CP apex, which allows calculation of the Turn Radius, R_{CP} .

$$R_{CP} = \frac{h}{\tan \delta_{CL}} \quad \text{eq. 4}$$

Equation 4 blows up (division by zero) if $\delta_{CL} = 0$ (neutral joystick position). So don't do **Snake Mode** calculations if the secondary joystick is neutral.

We need to now define γ_i . γ (no subscript) has already been defined as the angular offset between the chassis axis and the *vector of motion*. γ_i is the angular offset from the *vector of motion* to each individual pivot axis ($i = 1, 2, 3$). For calculation:

$$\gamma_1 = -\gamma \quad \text{eq. 5}$$

$$\gamma_2 = 120^\circ - \gamma \quad \text{eq. 6}$$

$$\gamma_3 = 240^\circ - \gamma \quad \text{eq. 7}$$

Turn radiuses for all swerve wheels may now be calculated:

$$R_i = \sqrt{h^2 \cos^2 \gamma_i + (R_{CP} - h \sin \gamma_i)^2} \quad \text{eq. 8}$$

and drive power factors for each wheel:

$$V_i = V \frac{R_i}{R_{\max}} \quad \text{eq. 9}$$

A choice is now needed. What will be the range of δ_{CL} ? In the first "*Pivot-Wheel Drive*" white paper of 2-August-2009, a limited (chassis aligned with *vector of motion*) **snake mode** was presented with a δ_{CL} range from -90° to $+90^\circ$. At the limits of the range, the turn radius is zero and the turn center-point and chassis center-point are the same. Swerve angle calculations were complicated by the need to switch calculations based on whether the turn center-point is inside or outside the wheel-base.

In "*Pivot-Wheel Drive - Crab with a Twist*" white paper of 29-March-2010, a general (random alignment between the chassis and *vector of motion*) **snake mode** (referred to as Twist 1 in the paper) was presented, but where δ_{CL} 's range is limited to -45° to 45° . By limiting the range of δ_{CL} , the turn center-point never comes inside of the h -radius circle around the chassis center-point; the equations are thereby simplified. The control logic for DEWBOTs IX & X both follow the mathematics presented in this latter paper, including the limited δ_{CL} range.

The math for both cases will be presented here.

For the case that:

$$\begin{aligned} [\text{sign of } \delta_{CL}] \cdot R_{CP} &\geq [\text{sign of } \delta_{CL}] \cdot h \sin \gamma_i && \text{(Turn center-point is not inside wheelbase -} \\ &&& \text{always true for } -45^\circ \leq \delta_{CL} \leq +45^\circ) \\ \delta_i &= [\text{sign of } \delta_{CL}] \sin^{-1} \frac{h \cos \gamma_i}{R_i} && \text{eq. 10} \end{aligned}$$

For the case that:

$$\begin{aligned} [\text{sign of } \delta_{CL}] \cdot R_{CP} &> [\text{sign of } \delta_{CL}] \cdot h \sin \gamma_i && \text{(Turn center-point is inside wheelbase)} \\ \delta_i &= 180^\circ - \tan^{-1} \left(\frac{h \cos \gamma_i}{R_{CP} - h \sin \gamma_i} \right) && \text{eq. 11} \end{aligned}$$

Finally, to calculate the actual steering set-points:

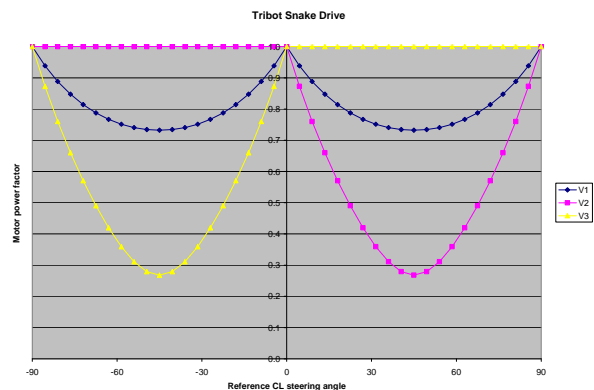
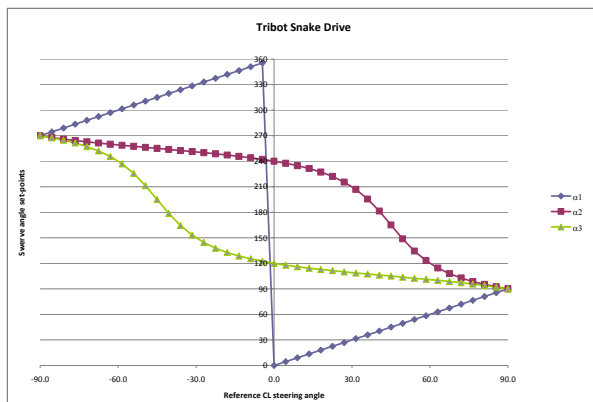
$$\alpha_i = \alpha_{Ci} + \delta_i \quad \text{(add or subtract } 360^\circ \text{ as needed for } 0\text{-}360^\circ \text{ range)} \quad \text{eq. 12}$$

A working Microsoft Excel model of *snake mode* control logic was developed.

Tribot Snake Mode Model

h	17.762 in	θ	0	120	240
γ	0°	α_{Ci}	0	240	120
		γ_i	0	120	240
		$h \sin \gamma_i$	0.000	15.382	-15.382
		$h \cos \gamma_i$	17.762	-8.881	-8.881

z	δ_{CL} (°)	R_{CP} (in)	R_{max} (in)	R_i (in)			δ_i			α_i			V_i		
				1	2	3	1	2	3	1	2	3	1	2	3
-1.00	90.0	0.000	17.762	17.762	17.762	17.762	90.00	210.00	-30.00	90.00	90.00	90.00	1.00	1.00	1.00
-0.95	85.5	1.398	18.985	17.817	16.566	18.985	85.50	212.42	-27.89	85.50	92.42	92.11	0.94	0.87	1.00
-0.90	81.0	2.813	20.247	17.983	15.390	20.247	81.00	215.24	-26.02	81.00	95.24	93.98	0.89	0.76	1.00
-0.85	76.5	4.264	21.561	18.267	14.230	21.561	76.50	218.62	-24.32	76.50	98.62	95.68	0.85	0.66	1.00
-0.80	72.0	5.771	22.942	18.676	13.086	22.942	72.00	222.74	-22.77	72.00	102.74	97.23	0.81	0.57	1.00
-0.75	67.5	7.357	24.412	19.225	11.970	24.412	67.50	227.90	-21.33	67.50	107.90	98.67	0.79	0.49	1.00
-0.70	63.0	9.050	25.997	19.935	10.907	25.997	63.00	234.51	-19.98	63.00	114.51	100.02	0.77	0.42	1.00
-0.65	58.5	10.885	27.728	20.832	9.955	27.728	58.50	243.14	-18.68	58.50	123.14	101.32	0.75	0.36	1.00
-0.60	54.0	12.905	29.649	21.955	9.220	29.649	54.00	254.41	-17.43	54.00	134.41	102.57	0.74	0.31	1.00
-0.55	49.5	15.170	31.817	23.359	8.884	31.817	49.50	268.63	-16.21	49.50	148.63	103.79	0.73	0.28	1.00
-0.50	45.0	17.762	34.314	25.119	9.194	34.314	45.00	-75.00	-15.00	45.00	165.00	105.00	0.73	0.27	1.00
-0.45	40.5	20.797	37.253	27.349	10.401	37.253	40.50	-58.63	-13.79	40.50	181.37	106.21	0.73	0.28	1.00
-0.40	36.0	24.447	40.808	30.219	12.690	40.808	36.00	-44.41	-12.57	36.00	195.59	107.43	0.74	0.31	1.00
-0.35	31.5	28.985	45.247	33.994	16.245	45.247	31.50	-33.14	-11.32	31.50	206.86	108.68	0.75	0.36	1.00
-0.30	27.0	34.860	51.021	39.124	21.407	51.021	27.00	-24.51	-10.02	27.00	215.49	109.98	0.77	0.42	1.00
-0.25	22.5	42.881	58.937	46.414	28.897	58.937	22.50	-17.90	-8.67	22.50	222.10	111.33	0.79	0.49	1.00
-0.20	18.0	54.666	70.609	57.479	40.275	70.609	18.00	-12.74	-7.23	18.00	227.26	112.77	0.81	0.57	1.00
-0.15	13.5	73.984	89.807	76.086	59.271	89.807	13.50	-8.62	-5.68	13.50	231.38	114.32	0.85	0.66	1.00
-0.10	9.0	112.145	127.836	113.543	97.169	127.836	9.00	-5.24	-3.98	9.00	234.76	116.02	0.89	0.76	1.00
-0.05	4.5	225.688	241.233	226.385	210.493	241.233	4.50	-2.42	-2.11	4.50	237.58	117.89	0.94	0.87	1.00
0.00	0.0	∞	∞	∞	∞	∞	0.00	0.00	0.00	0.00	240.00	120.00	1.00	1.00	1.00
0.05	-4.5	-225.688	241.233	226.385	241.233	210.493	-4.50	2.11	2.42	355.50	242.11	122.42	0.94	1.00	0.87
0.10	-9.0	-112.145	127.836	113.543	127.836	97.169	-9.00	3.98	5.24	351.00	243.98	125.24	0.89	1.00	0.76
0.15	-13.5	-73.984	89.807	76.086	89.807	59.271	-13.50	5.68	8.62	346.50	245.68	128.62	0.85	1.00	0.66
0.20	-18.0	-54.666	70.609	57.479	70.609	40.275	-18.00	7.23	12.74	342.00	247.23	132.74	0.81	1.00	0.57
0.25	-22.5	-42.881	58.937	46.414	58.937	28.897	-22.50	8.67	17.90	337.50	248.67	137.90	0.79	1.00	0.49
0.30	-27.0	-34.860	51.021	39.124	51.021	21.407	-27.00	10.02	24.51	333.00	250.02	144.51	0.77	1.00	0.42
0.35	-31.5	-28.985	45.247	33.994	45.247	16.245	-31.50	11.32	33.14	328.50	251.32	153.14	0.75	1.00	0.36
0.40	-36.0	-24.447	40.808	30.219	40.808	12.690	-36.00	12.57	44.41	324.00	252.57	164.41	0.74	1.00	0.31
0.45	-40.5	-20.797	37.253	27.349	37.253	10.401	-40.50	13.79	58.63	319.50	253.79	178.63	0.73	1.00	0.28
0.50	-45.0	-17.762	34.314	25.119	34.314	9.194	-45.00	15.00	75.00	315.00	255.00	195.00	0.73	1.00	0.27
0.55	-49.5	-15.170	31.817	23.359	31.817	8.884	-49.50	16.21	91.37	310.50	256.21	211.37	0.73	1.00	0.28
0.60	-54.0	-12.905	29.649	21.955	29.649	9.220	-54.00	17.43	105.59	306.00	257.43	225.59	0.74	1.00	0.31
0.65	-58.5	-10.885	27.728	20.832	27.728	9.955	-58.50	18.68	116.86	301.50	258.68	236.86	0.75	1.00	0.36
0.70	-63.0	-9.050	25.997	19.935	25.997	10.907	-63.00	19.98	125.49	297.00	259.98	245.49	0.77	1.00	0.42
0.75	-67.5	-7.357	24.412	19.225	24.412	11.970	-67.50	21.33	132.10	292.50	261.33	252.10	0.79	1.00	0.49
0.80	-72.0	-5.771	22.942	18.676	22.942	13.086	-72.00	22.77	137.26	288.00	262.77	257.26	0.81	1.00	0.57
0.85	-76.5	-4.264	21.561	18.267	21.561	14.230	-76.50	24.32	141.38	283.50	264.32	261.38	0.85	1.00	0.66
0.90	-81.0	-2.813	20.247	17.983	20.247	15.390	-81.00	26.02	144.76	279.00	266.02	264.76	0.89	1.00	0.76
0.95	-85.5	-1.398	18.985	17.817	18.985	16.566	-85.50	27.89	147.58	274.50	267.89	267.58	0.94	1.00	0.87
1.00	-90.0	0.000	17.762	17.762	17.762	17.762	-90.00	30.00	150.00	270.00	270.00	270.00	1.00	1.00	1.00



Chassis-centric Ocelot Mode

Presently, *ocelot mode* requires that the driver dynamically rotate the vector of motion (using the primary joystick) to maintain a steady course while snake steering. This should work with the control equations presented here, although care needs to be taken to keep the turn center-point away from the chassis center-point. Otherwise the robot will spin in a stationary location. I understand that the current *ocelot drive* (4-wheel) basically “rolls” along the h radius circle which passes through the pivot axes.

Field-centric Control

Field-centric control requires that the robot be able to sense the direction of the field axis relative to chassis orientation (ϕ). Typically this requires a gyroscope (ideally at the chassis center-point) although other options exist. This sensing need be only one axis.

If using a gyroscope, concerns are:

1. Stability of the gyroscope over the match duration
2. Initializing and calibrating the control system to the field axis at match start.

We need to understand what chassis orientation behavior we want in field-centric control. We know from chassis-centric experience that the orientation relative to the field changes as we drive. We could accept this; using the gyroscope to control speed and direction relative to the field but allow orientation to drift as we drive and then control it using the secondary joystick only as and when needed, or we could use the gyroscope data to control chassis orientation unless the secondary joystick is used to change it.

Field-centric Crab Mode

There needs to be an additional piece of information: ϕ ($^{\circ}$), the angular displacement of the field axis from the chassis axis (0-360 $^{\circ}$).

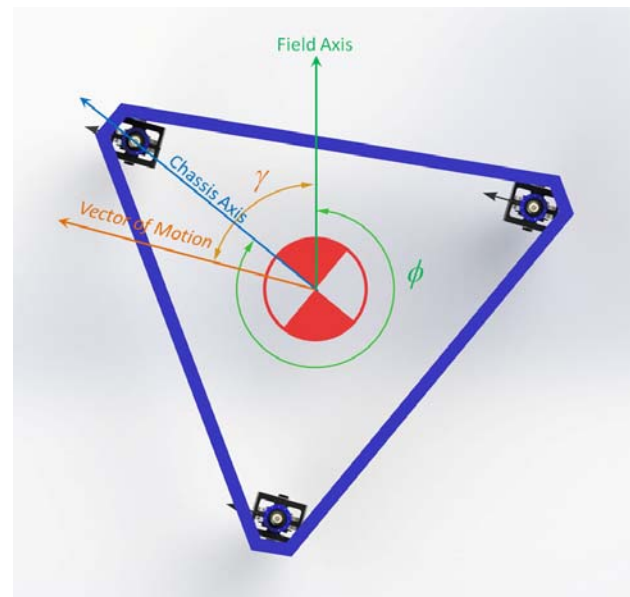
The joystick steering direction, γ ($^{\circ}$), is now relative to the field axis, not the chassis axis.

For crab mode, swerve set-points can be calculated:

$$\alpha_{C1} = \gamma + \phi \quad \text{eq. 13}$$

$$\alpha_{C2} = \gamma + \phi - 120^{\circ} \quad \text{eq. 14}$$

$$\alpha_{C3} = \gamma + \phi - 240^{\circ} \quad \text{eq. 15}$$



As with chassis-centric crab mode, these values need to be checked and adjusted to 0-360° range.

All drive motors are driven at the same power on *crab mode* based on primary joystick displacement from neutral.

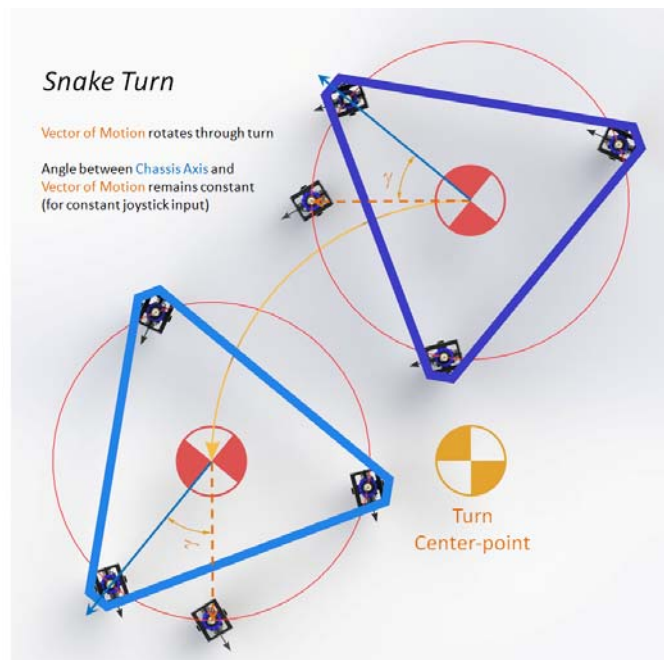
Field-Centric Chassis Orientation

The action of the secondary joystick is fundamentally different in field-centric control than it is in chassis-centric. In chassis-centric control, this input drives the robot in *snake* turns. In field-centric, the secondary joystick rotates the chassis to change chassis orientation while driving in *crab mode*. This is an *ocelot twist* and this drive mode is automatic in field-centric control. In chassis-centric, *ocelot twist* driving requires dynamic driver control. In field-centric control, it is *snake turning* which requires dynamic driver control. They are flipped.

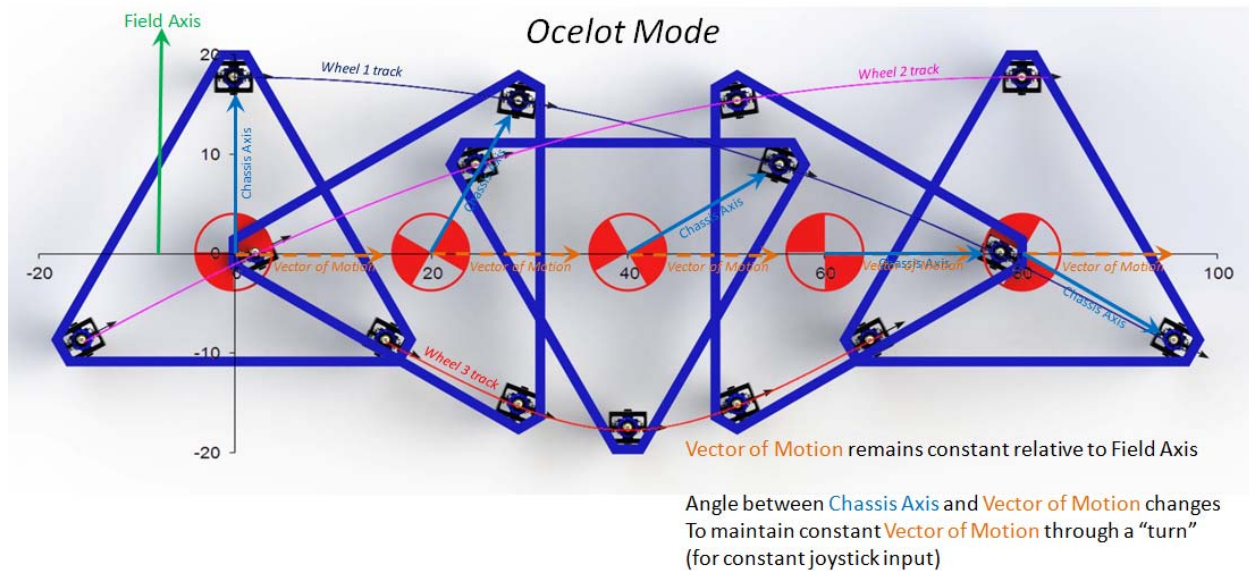
The white paper "*Pivot-Wheel Drive - Crab with a Twist*" of 29-March-2010 dealt with *ocelot mode* (referred to as Twist 2 in the paper), but not effectively. A different approach is used here.

Actually, an *ocelot* twist is handled just like a *snake* turn, but with a critical difference:

- In a *snake* turn, for a given joystick input, the angle between the *vector of motion* and the chassis axis remains fixed and the *vector of motion* rotates about a turn center-point. Swerve set-points during a *snake* turn are static - they are determined by the joystick input only and do not change until the joystick input changes.
- An *ocelot* twist, for a given joystick input, maintains a constant *vector of motion* relative to the field axis. While the turn logic and mathematics are the same as snake, an actual turn is prevented by continually adjusting wheel directions to keep the robot's course constant. This is a dynamic steering system.



As with *snake* turning, a "reference CL wheel" is used for steering. The steering angle (δ_{CL}) range for this wheel should definitely be constrained to $\pm 45^\circ$. δ_{CL} is determined directly by the secondary joystick x input (just as in *snake*) and determines (for a fixed speed input) the rotational speed of the *ocelot* twist. Note that *ocelot* twisting will slow the robot's overall velocity and this effect increases as δ_{CL} deviates from 0° .



Variables & calculations:

ϕ was defined in the Field-Centric Crab Mode section as the angle between the chassis axis and the field axis. This is provided in real time via on-board instrumentation. It is dynamic.

γ was defined in the Field-Centric Crab Mode section as the steering direction relative to the field axis. This is provided from the primary joystick. Static (as long as joystick input not changed).

α_{C1} , α_{C2} and α_{C3} have been defined in equations 13, 14 & 15 in the Field-Centric Crab Mode section. These are the swerve angle set-points for Field-Centric Crab Mode. Dynamic.

R_{CP} (in) is calculated using equation 4 in the Chassis-Centric Snake Mode section. Even though we're not actually turning, we run the math as if we are. Static (as long as joystick input not changed).

γ_i (defined in the Chassis-Centric Snake Mode section) remains the angular offset between the *vector of motion* and each individual pivot axis ($i = 1, 2, 3$). Dynamic. The calculation of these values changes under field-centric control:

$$\gamma_1 = -\phi - \gamma \quad \text{eq. 16}$$

$$\gamma_2 = 120^\circ - \phi - \gamma \quad \text{eq. 17}$$

$$\gamma_3 = 240^\circ - \phi - \gamma \quad \text{eq. 18}$$

R_i (in) are the individual wheel distances from the "turn center-point" ($i = 1, 2, 3$) and are calculated using equation 8. Dynamic.

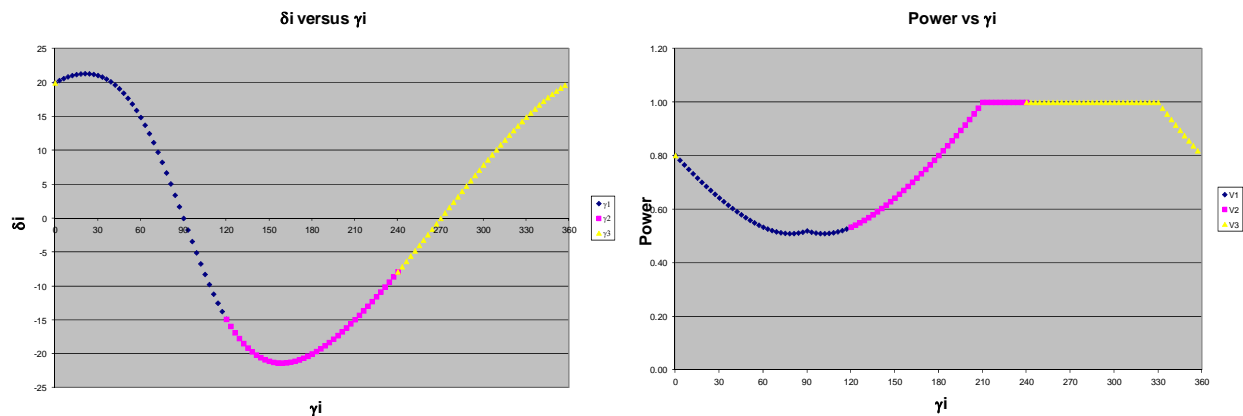
V_i are the individual wheel power factors ($i = 1, 2, 3$) and may be calculated using equation 9. Dynamic.

δ_i ($^\circ$) are the individual swerve angle "corrections" (from the base α_{Ci} 's) needed to affect the *ocelot* twist ($i = 1, 2, 3$). Calculated from equation 10 and are not conditional as long as $-45^\circ \leq \delta_{CL} \leq +45^\circ$. Dynamic.

α_i ($^\circ$) are the swerve angle set-points ($i = 1, 2, 3$). Calculated using equation 12. Dynamic.

So almost all of the mathematics are recycled from *snake mode*.

A robust Microsoft Excel model of field-centric *ocelot mode* control logic was developed, but it's a little heavy to paste in a Microsoft Word document. An observation is warranted, though. The plots of δ_i versus γ_i and V_i versus γ_i are very characteristic and regular for a given δ_{CL} . Examples below. There may be an opportunity to reduce some calculation burden with look-up tables. Something to keep in mind.



A Final Twist in our Story

The final twist is a stationary twist around the chassis center-point. Swerve angles would all be 90° or 270° , depending upon the direction of the twist. We do this now (DEWBOT X). We'll need to do it with a 3-swerve robot as well. This is referred to as Twist 3 in "*Pivot-Wheel Drive - Crab with a Twist*" of 29-March-2010.